

Rješenja problema i zadataka za treći razred

Modul 1

Problemi:

6. c) 8. a) 11. d) 23. b) 28. d) 36. c) 37. b) 38. a) 41. a)
42. a) 46. a) $tg\varphi < 0 \Rightarrow R_L < R_C$; b) $tg\varphi = 0 \Rightarrow R_L = R_C$; c) $tg\varphi > 0 \Rightarrow R_L > R_C$ 51. c)
57. $E_k = 3E_{ep}$ 64. $T_1 = 2T_0$, $T_2 = T_0/2$ 65. $T_a = T_b = T_c$ 70. d) 71. $y = 2\text{cmsin}(\pi s^{-1}t + \pi)$
72. $x_0 = 10\text{cm}$, $T = 8\text{s}$, $f = 0,125\text{Hz}$
75. i) a), c), d), f); ii) $x = 0$, $v = v_0$, $a = 0$, $F = 0$, $E_k = E_{k0}$, $E_{ep} = 0$

Zadaci:

77. c) 78. $v = 240\text{m/s}$ 79. a) $\Phi = 5 \cdot 10^{-4}\text{Wb}$; b) $U_i = 10\text{mV}$ 80. $\Delta t = 3,43\mu\text{s}$
81. $U_i = 0,1\text{V}$ 82. $U_i = 1,88\text{mV}$ 83. $U_i = 4,71\text{V}$ 84. $I_i = 0,365\text{A}$ 85. $U_i = 40,69\text{mV}$
86. $U_L = 0,5\text{V}$ 87. $L = 3,89\text{mH}$ 88. $\mathcal{E}_L = 125\text{V}$ 89. $L = 3\text{H}$
90. $\mathcal{E}_1 = -0,6\text{V}$, $\mathcal{E}_2 = 0,6\text{V}$; $I_1 = -6\text{A}$, $I_2 = 6\text{A}$ 91. $\Delta I/\Delta t = 50\text{A/s}$ 92. 100 puta u 1s, $t = 5\text{ms}$
93. $U = 220\text{V}$, $U_0 = 311\text{V}$, $I = 0,1136\text{A}$, $I_0 = 0,16\text{A}$
94. $f = 50\text{Hz}$, $I_0 = 2,8\text{A}$, $I = 1,98\text{A}$, $U_0 = 280\text{V}$, $U = 198\text{V}$ 95. $u = 314\text{V sin}(628t + \pi/4)$
96. $\varphi = \pi/3$, $U_0 = 11,5\text{V}$ 97. $t = 12,2\text{ms}$ 98. $U_2 = 13,2\text{kV}$ 99. e) 100. $I_2 = 50\text{A}$
101. $N_2 = 12$ 102. i) $N_2/N_1 = 50$, ii) $U_2' = 4,8\text{V}$ 103. b) 104. e) 105. b)
106. $R = 3,626\Omega$ 107. $I = 5,02\text{A}$, $f = 50\text{Hz}$, $U_L = 157,63\text{V}$ 108. $C = 7,2\mu\text{F}$
109. $R_L/R_C = 1,97 \cdot 10^{-2}$ 110. $Z = 111,8\Omega$, $I = 1,968\text{A}$ 111. $\cos\varphi = 0,894$, $P_a = 387\text{W}$
112. $C = 28,2\mu\text{F}$ 113. $\varphi = 0,6435$ ($\varphi = 36^\circ 52'$) 114. $I = 2,04\text{A}$ 115. $C = 1,58\mu\text{F}$
116. $C = 5,07\mu\text{F}$ 117. b) 118. $f = 10\text{Hz}$, $N = 300$ 119. $k = 54,78\text{N/m}$
120. $\Delta l = 6,2\text{cm}$ 121. $m_2/m_1 = 5/4$ 122. $T = 1,4\text{s}$, $f = 0,714\text{Hz}$, $\omega = 4,486\text{rad/s}$
123. $T = 0,628\text{s}$ 124. b) 125. $y_0 = 19,6\text{cm}$, $T = 0,888\text{s}$, $f = 1,126\text{Hz}$
126. $l = 21,2\text{cm}$ 127. $T = 0,565\text{s}$ 128. $T = 0,628\text{s}$ 129. b) 130. $E_{ep0} = E_{k0} \equiv E = 0,5\text{J}$
131. e) 132. $k = 400\text{N/m}$ 133. $E_{ep} = 22,6\text{mJ}$ 134. c) 135. $y = 5\text{cmsin}\pi/2 \cdot s^{-1}t$
136. tablica i graf 137. $y = 5\text{cmsin}4\pi s^{-1}t$ 138. c) 139. $y_0 = 0,75\text{cm}$, $T = 0,2\text{s}$, $f = 5\text{Hz}$
140. $y = 2\text{cmcos } 10\pi s^{-1}t$ 141. i) $y_{0A} = 2,5\text{m}$, $T_A = 4\text{s}$, $f_A = 0,25\text{Hz}$, $y_A = 2,5\text{msin}\pi/2 \cdot s^{-1}t$
ii) $y_{0B} = 3,5\text{m}$, $T_B = 2\text{s}$, $f_B = 0,5\text{Hz}$, $y_B = 3,5\text{mcos}\pi s^{-1}t$
142. $f = 0,5\text{Hz}$, $y(2,75\text{s}) = 7\text{mm}$ 143. $y(T/6) = 4,33\text{cm}$ 144. $t = 0,25\text{s}$
145. $t = 0,04\text{s}$, $y = 2,4\text{cm}$ 146. $y = 2,165\text{cm}$ 147. $t = 0,062\text{s}$ 148. $t = 0,1047\text{s}$
149. $v = 1,73\text{m/s}$ 150. $v = 2\pi\text{m/s cos}(\pi/2 \cdot s^{-1}t \pm \pi)$, $a = -\pi^2\text{m/s}^2\text{sin}(\pi/2 \cdot s^{-1}t \pm \pi)$
151. $y = 17,32\text{cm}$, $y' = 10\text{cm}$ 152. a) $k = 39,24\text{N/m}$; b) $v_0 = 0,7\text{m/s}$, $E_{k0} = 4,9 \cdot 10^{-2}\text{J}$

Modul 2

Problemi:

5. b) 9. b) 10. e) 11. ($g_Z > g_M$) $\Rightarrow f_Z > f_M$ 12. $T_p < T_e \Rightarrow$ brže "ide" na polu
13. Za jednostavno njihalo: $T_M = T_Z$, T elastične opruge s utegom ne ovisi o g 15. $l_2 = 4l_1$
31. $T_2 = T_1\sqrt{2}$ 35. a) 58. slobodan 63. $v_B > v_A$ 71. i 72. načelo superpozicije

Zadaci:

78. $t = 0,45s$ 79. c) 80. b) 81. $T_M = 4,94s$ 82. $T_M = 4,9s$
83. $y = 17,7cm$, $v = -0,224m/s$, $a = -0,1037m/s^2$ 84. a) $T_1 = T = 1s$; b) $a = 7,36m/s^2$ (gore)
85. $g = 9,655m/s^2$ 86. $l = 12cm$ 87. $f = 1,115Hz$ 88. $T = 1,7s$ 89. $k_2 = 2,5N/m$
90. $T = 2,96\mu s$, $f = 0,34MHz$ 91. $L = 2,5\mu H$ 92. e) 93. b) 94. $C = 3,5pF$
95. a) $I_0 = 0,64A$, $Q_0 = 1,2mC$, $E_{e0} = 7,2mJ$; b) $i(t) = -0,32A$, $q(t) = 1,039mC$ 96. $T = 25,12ns$
97. $C = 22,5nF$ 98. $f = 0,796MHz$ 99. $v = 20m/s$ 100. $v_1 = 1,25v_2$ 101. $t = 1,749s$
102. $F = 187,5N$ 103. $f = 3,5Hz$ 104. $m_2 = 50,97kg$ 105. $E = 9,85 \cdot 10^{10}N/m^2$
106. $\Delta v = 0,4m/s$ 107. $f = 5Hz$
108. $y_0 = 0,06m$, $\lambda = 8cm$, $f = 3,75kHz$, $y = 0,06m\sin 2\pi(7500\pi s^{-1}t - x/0,08m)$
109. a) $y_0 = 5cm$; b) $\lambda = 0,4m$; c) $v = 12m/s$; d) $f = 30Hz$; e) $v_0 = 9,42m/s$; f) $\varphi_0 = \pi/4$,
g) $y = 5cm\sin 2\pi(30s^{-1}t - 2,5m^{-1}x + 1/8)$ 110. $y = -0,924m$
111. $y = 0,2m\sin 2\pi(t/2s - x/400m)$
112. a) $y_0 = 3mm$; b) $f = 60Hz$; c) $T = 16,7ms$; d) $\lambda = 2cm$; e) $v = 1,2m/s$
113. $\lambda = 4cm$, $y_0 = 2cm$, $y = 2cm\sin 2\pi(t/0,3s + x/4cm \pm 1/2)$ (val se širi u smjeru negativne x -osi)
114. $\lambda = 0,6m$, $y_0 = 2m$, $y = 2m\sin 2\pi(t/0,03s - x/0,6m)$
115. $T = 0,1s$, $f = 10Hz$, $y = 2m\sin 2\pi(t/0,1s - x/30m)$
116. $T = 2s$, $f = 0,5Hz$, $y = 2m\sin 2\pi(t/2s - x/400m + 1/4)$ 117. $y = 1,41cm$
118. i 119. uraditi tablicu elongacije i nacrtati graf 120. $y = 0$
121. $y(x,t) = 2cm\sin(2\pi s^{-1}t + \pi/2)$ - nacrtati graf
122. a) $y_0 = 2cm$; b) $\lambda = 3cm$; c) $f = 1kHz$; d) $v = 30m/s$
123. a) $x_1 = 4m$; b) $x_2 = 2m$; c) $x_3 = 6m$
124. a) $y_0 = 0,05m$; b) $\omega = 2\pi rad/s$, $f = 1Hz$, $T = 1s$; c) $v = 2m/s$ (udesno); d) $\Delta\varphi = 3\pi/2$
125. d) 126. $\Delta\varphi = 1,33\pi(240^\circ)$ 127. $d = 120m$ 128. b)
129. $\lambda \equiv d = 25m$, $f = 0,25Hz$, $v = 6,25m/s$ 130. $v_{mol} = 0,94m/s$, $v_v = 6,25m/s$
131. $v_v = 6,63v_{mol}$ 132. $\lambda_v = 3,4m$, $\beta = 50^\circ$ 133. $\beta = 70^\circ 30'$ 134. $\beta = 51^\circ 2'$, $\alpha_{max} = 12^\circ 54'$
135. a) ($k=2$) 136. $\Delta s = 6\lambda$ (registriraćemo maksimalnu jakost zvuka)
137. Ispunjen je uvjet za destruktivnu interferenciju: $\Delta s = (2k-1)\lambda/2$, $k=3 \Rightarrow$ magarac neće čuti zvuk.
138. $\lambda = 2m$ 139. c) 140. $\lambda = 0,6m$, $v = 6m/s$ 141. $f_{min} = v/0,5m$ 142. $f_1 = 2,5Hz$

Modul 3

Problemi:

7. $v_{H_2} > v_{CO_2}$, $v_{H_2} = 4,69v_{CO_2}$ 26. a) 27. $f_{min} = v/2l$ 29. $f_2 = 2f_1$ 34. $f_{1o} = 2f_{1z}$
40. a) u točki A; b) u točki C 55. slušatelj radija čije je uho uz zvučnik radija, ($c \gg v_{zrak}$)
67. $\alpha + \beta = 90^\circ$, $\alpha = \beta \Rightarrow \alpha = 45^\circ$
72. Neće vidjeti strelicu u potpunosti već samo njezin vrh (nacrtaj). 73. $x' = -x$
75. Konkavno zrcalo služi kao povećalo jer može dati uvećanu (virtualnu) sliku.

Zadaci:

80. $\lambda_{min} = 1,7cm$, $\lambda_{max} = 17m$ 81. $\lambda \in (72cm - 2,27m)$ 82. $t = 1,336s$ 83. $F = 80N$
84. $v_2/v_1 = 2,45$ 85. $E = 1,68 \cdot 10^{11}Pa$ 86. $v_1 = 490m/s$, $v_2 = 0$ 87. $d = 1721,2m$
88. $\Delta v = 6m/s$ 89. $\delta v (\%) = 4,9 \%$ 90. $v = 1924,1m/s$ 91. $\lambda = 1,22m$ 92. a)
93. $I = 0,54W/m^2$ 94. $y_0 = 107,5nm$ 95. $\Delta I/I_1 (\%) = 99,9\%$ 96. $E = 2\mu J$ 97. $L = 17dB$
98. $I_1 = 10^{-11}W/m^2$, $I_2 = 10^{-6}W/m^2$, $I_3 = 1W/m^2$ 99. $L = 77dB$ 100. $L = 40dB$
101. $I_2 = 100I_1$ 102. $l_2/l_1 = 0,5$ 103. $f_1 = 156,5Hz$, $f_2 = 313Hz$, $f_3 = 469,5Hz$
104. $\lambda_{max} = 0,5m$ 105. $f_1' = 400Hz$ 106. $f_1 = 2,5Hz$ 107. $E = 1,584 \cdot 10^{10}Pa$
108. i) $\lambda_1 = 8m$, $f_1 = 625Hz$ ii) $\lambda_2 = 2,667m$, $f_2 = 1875Hz$ 109. $l_{niže} = 7,5m$
110. $f_3 = 18,56Hz$, i) $s_{1\varepsilon} = l/3 = 0,267m$, $s_{2\varepsilon} = 2l/3 = 0,533m$, $s_{3\varepsilon} = l = 0,8m$,
ii) $s_{1tr} = l/6 = 0,133m$, $s_{2tr} = l/2 = 0,4m$, $s_{3tr} = 5l/3 = 0,667m$ 111. $l = 18,6cm$
112. c) 113. $l \equiv h = 16,6cm$ 114. a)
115. $\lambda_1 = 1,52m$, $f_1 = 223,68Hz$, $\lambda_2 = 0,76m$, $f_2 = 447,36Hz$ 116. c)
117. $f_{min,o} = 144,58Hz$, $f_{min,z} = 72,29Hz$ 118. $f' = 1133,3Hz$
119. $f' = 630Hz$, $f'' = 570,27Hz$ 120. $v_z = 1039,5km/h$ 121. $v_b = 4,95m/s$
122. $\Delta f = 571,4Hz$ 123. $f'' = 42,8Hz$ 124. $v_k = 3,317m/s$, ($v_{krel} = 1,68m/s$)
125. $v_o = 0,185c$ 126. $\lambda = 0,57m$ (radioval) 127. $\lambda = 0,674m$ 128. $\varepsilon_r = 81$
129. a) $\lambda = 30m$, $T = 10^{-7}s$; b) $E = 5V/m$ 130. $\lambda = 29,8m$ 131. $f = 1,25 \cdot 10^8Hz$
132. $\lambda_0 = 3 \cdot 10^{-6}m$, $v = 3,83 \cdot 10^7m/s$ 133. $I_0 = 0,64A$, $Q_0 = 1,2mC$, $E_{ep0} = 7,2mJ$
134. $\gamma = 20^\circ$ 135. $x = 0,86m$ 136. $x = 60cm$, $x' = 30cm$ 137. $t = 0,714s$
138. $R = 0,8m$
139. $x' = -15cm$, $y' = 6cm$ (slika je virtualna ($x' < 0$), uspravna ($y' > 0$) i uvećana ($y' > y$)).
140. $x = 60cm$, $x' = 30cm$ 141. $y = 1cm$ 142. i) $x = 0,75m$, ii) $x = 1,25m$ 143. $f = 40cm$
144. $R \approx 1,03cm$ 145. $x' = 11,11cm$ ($x' < 0$), $m = 0,56$ 146. $x = 50cm$ 147. $x = 5m$

Modul 4

Problemi:

6. a) 8. Koristiti transformaciju $\sin \alpha \approx \tan \alpha$ (za male kutove) $\Rightarrow n_2 \tan \alpha = n_1 \tan \beta \Rightarrow h' = hn_2/n_1$
23. $f_1 = 20\text{cm}$, $f_1 = -50\text{cm}$
25. Uranjanjem u vodu jakost leće se smanjuje tj. povećava se žarišna daljina.
45. $m_{1,1} = 50$, $m_{1,2} = 100$, $m_{1,3} = 150$, $m_{2,1} = 100$, $m_{2,2} = 200$, $m_{2,3} = 300$, $m_{3,1} = 200$, $m_{3,2} = 400$, $m_{3,3} = 600$,
48. $k = 5 \Rightarrow$ a) 49. $n_2 < n_1$, $\delta s = 2\lambda$ (konstruktivna interferencija)

Zadaci:

68. $n = 1,333$ 69. $v = 2 \cdot 10^8 \text{m/s}$ 70. $v = 2,25 \cdot 10^8 \text{m/s}$ 71. $d_v/d_u = 1,1$
72. $\lambda = 333, 3\text{nm}$ 73. $\alpha = 41^\circ 40'$ 74. $\beta = 6^\circ 38'$, $\beta' = 9^\circ 56'$, $\beta'' = 16^\circ 22'$
75. $\Delta\beta \equiv \beta_{lj} - \beta_c = 2^\circ 38'$ 76. $\beta = 50^\circ 9'$ 77. $n_t = 1,47$, $v_t = 0,68c$ 78. $l = 0,858\text{m}$
79. $l = 2,95\text{m}$ 80. $n_s = 1,5$ 81. b) 82. $\alpha_{gr} = 48^\circ 33'$, $v = 0,75c$ 83. $n_1 = 1,62$
84. $\alpha_{gr} = 61^\circ 2'$ 85. $n_s = 1,52$ 86. $n = 1,37$ 87. e) 88. $d = 10\text{mm}$ 89. $\delta = 4,42\text{cm}$
90. $n_{min} = 1,414$ 91. $\delta = 16^\circ 14'$ 92. $\varepsilon = 43^\circ$ 93. $\varepsilon = 38^\circ 58'$ 94. $\Delta\beta \equiv \beta_{lj} - \beta_c = 4^\circ 10'$
95. $R = 14\text{cm}$ 96. $R = 15,39\text{cm}$ 97. a) $x' = -4\text{m}$; b) $x' = 3\text{m}$
98. $x' = 60\text{cm}$ (slika je realna) 99. $x' = -20\text{cm}$, $y' = 2,5\text{cm}$ 100. $x_1 = 30\text{cm}$, $x_2 = 10\text{cm}$
101. $f = 26,67\text{cm}$ 102. d) 103. $d = 40\text{cm}$ 104. $x = 75\text{cm}$
105. $x_1 = 49,25\text{cm}$, $x_2 = 16,75\text{cm}$ 106. $x = 2\text{m}$ 107. $m = 6$
108. $x' = 28,57\text{cm}$ ($x' < 0 \Rightarrow$ slika je virtualna) 109. $x' = 6\text{cm}$ (slika je virtualna i uspravna), $m = 0,4$
110. $x' = 15\text{cm}$ ($x' < 0 \Rightarrow$ slika je virtualna i uspravna), $m = 0,25$, $y' = 1\text{cm}$, $j = -5\text{m}^{-1}$
111. $x = 10\text{cm}$ 112. $f = 12\text{cm}$ ($f < 0$) 113. $x' = 12,5\text{cm}$, $y' = 1\text{cm}$ 114. a) 115. a)
116. $j = -1,25D$ 117. b) 118. $j = 2,67D$ 119. b) 120. $s_{1c}/s_{1lj} = \lambda_c/\lambda_{lj}$
121. $\lambda = 580\text{nm}$ 122. $\Delta s_3 = 4,558\text{cm}$ 123. $a = 1,6\text{m}$ 124. $\lambda = 667\text{nm}$
125. $s_2 = 4,48\text{cm}$, $\Delta s = 2,24\text{cm}$ 126. $r_2 = 1503\lambda$ 127. b) 128. $d = 0,58\text{mm}$
129. $\lambda' = 576,87\text{nm}$ 130. $\lambda = 624\text{nm}$, $f = 4,8 \cdot 10^{14}\text{Hz}$ 131. $\lambda = 698\text{nm}$ 132. $\alpha_4 = 2^\circ 45'$
133. $\lambda = 600\text{nm}$ 134. $\Delta\alpha = \alpha_{3c} - \alpha_{3lj} = 18^\circ 12'$ 135. $\lambda = 500\text{nm}$ 136. $\alpha_3 = 48^\circ 35'$
137. $\alpha_1 = 22^\circ 19'$, $\alpha_2 = 42^\circ 24'$, α_3 ne postoji 138. $f = 5,69 \cdot 10^{14}\text{Hz}$ 139. $\alpha = 10^\circ 14'$
140. $k_{max} = 4$, $\alpha_4 = 70^\circ 27'$ 141. $k_{max} = 7$, $\alpha_7 = 64^\circ 54'$ 142. $n_2 = 1,58$ 143. $\gamma = 36^\circ 57'$
144. $n_t = 1,33$ 145. a) $\alpha = 56^\circ 19'$; b) $\alpha' = 44^\circ 49'$

Modul 5

Problemi:

6. Pogrešno je, pri tako velikim brzinama, koristiti relacije klasične fizike. 7. $v_x = c$
8. Prema relativističkoj relaciji slaganja \Rightarrow : Ako je jedna ili obje brzine jednaka c njihov zbroj ne može dati rezultat $v > c$.
12. c) 13. c) 36. a) 42. najveći je u slučaju c) a najmanji u slučaju a) 57. a)
58. c) 61. $W_1/W_2 = 4$ 62. b)

Zadaci:

63. $x' = 2,3km$, $t' = 3,08 \cdot 10^{-5}s$ 64. $v_x = 0,97c$ 65. $v_x = -c$ 66. $v_x = 0,727c$
67. $v_{x1} = v_{x2} = c$ 68. $v_x = 0,143c$ 69. c) 70. $v = 0,943c$ 71. $\delta l \equiv \Delta l/l_0 = 20\%$
72. $v = 0,6c$ 73. $l = 0,436m$ 74. $P = 72cm^2$ 75. $l_0 = 15,27m$, $\alpha' = 19^\circ 6'$ 76. c)
77. a) $s_0 = 9,36 \cdot 10^{15}m$; b) $s = 6,62 \cdot 10^{16}m$ 78. $\Delta t = 7,07s$ 79. $\Delta t = 4god$ 80. $v = \sqrt{3} c/2$
81. $E_0 = 8,19 \cdot 10^{-14}J$, $p = 5,63 \cdot 10^{-22}kgm/s$ 82. $v = 0,967c$ 83. $v = 0,995c$
84. $\Delta t/\Delta t_0 = 20$ 85. $\Delta t_0 = \Delta t/8$ 86. $E/E_0 = 2$ 87. $v = 0,998c$ 88. $v = 2\sqrt{2} c/3$
89. $E_k = 5,46 \cdot 10^{-14}J$ 90. $v = 0,95c$ 91. $p = 4,728 \cdot 10^{-22}kgm/s$ 92. $v_e = 0,878c$
93. $p = 9 \cdot 10^{-19}kgm/s$ 94. $U = 215kV$ 95. $\omega = 40rad/s$ 96. c) 97. $N = 15,92okr.$
98. $\alpha = 0,157rad/s^2$, $N = 5$ 99. $\alpha = 21,6rad/s^2$ 100. $\alpha = 2,4\pi rad/s^2$, $a = 7,54m/s^2$
101. $\varphi = 3 (rad)$, $\omega = 0,7rad/s$ 102. $\omega = 1rad/s$
103. $M_a) = 0$, $M_b) = 0,707Nm$, $M_c) = 0$ 104. $F_{min} = 14,14N$ 105. $l_1 = 9cm$, $l_2 = 5cm$
106. $F = 654N$ 107. $x = 2,045m$ (od težeg dječaka) 108. $l_1 = 1m$, $l_2 = 2m$
109. Hoće, $M_v(600Nm) > M_g(490,5Nm)$ 110. $F_N = 1510,7N$ 111. $x = 3m$
112. $M = 43,96N$ 113. $M_{tr} = 1Nm$ 114. $I = 0,64kgm^2$ 115. $m = 340,4kg$, $N \approx 15$
116. $I = 9,52kgm^2$ 117. a) 118. $M = 0,04Nm$ 119. $\varphi = 4930 (rad)$
120. $L = 21,195kgm^2/s$ 121. $v_{CMpl.} = 3,2m/s$, $\omega_{pl.} = 10,67rad/s$ 122. $f_2 = 0,88okr./s$
123. $\omega = 46rad/s$ 124. $E_{krot.} = 4,92kJ$ 125. $E_k = 2352J$ 126. $E_{krot.} = 197,2kJ$
127. $a_k > a_o$ 128. $W = 23,15J$, $v = 1,183m/s$ 129. $\Delta E_{krot.} = 163,225J$ 130. $v = 5,6m/s$

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